

Object-Oriented Modelling in LePUS3 and Class-Z

- Modelling small programs
- Modelling large programs
- Modelling application frameworks
- Modelling design patterns

LePUS3 and Class-Z: desiderata

- Abstraction
 - Abstract ontology
 - Offer an answer: What are the conceptual building blocks of software design?
 - Scaling: capture the building blocks of very large programs
 - Detailed notation—cluttered diagrams
 - What NOT to model? What a specification should NOT represent?
- Rigour
 - Formal specification
 - Verification
- Decidability: Tool support in "round-trip engineering"
 - automated verification is possible in principle
 - Tool support automates the verification process
 - Allows us to "close the loop" of round-trip engineering
- Visualization (Optional)
 - Offer a "picture" of a specification:
 - Existing program: a 'roadmap' to the millions of lines of code
 - A design motif: design pattern, architectural style
 - Makes software easier to understand and change
- Theory & practice
 - Be relevant to practical applications
 - Provide a sound foundation in a solid mathematical theory

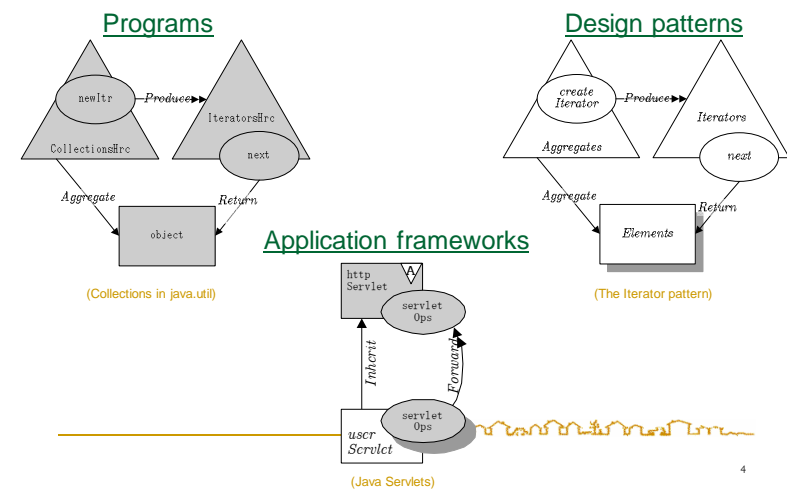
Specification language: desiderata (cont.)

- Combine theory & practice

It has long been my personal view that the separation of practical and theoretical work is artificial and injurious. Much of the practical work done in computing, both in software and in hardware design, is unsound and clumsy because the people who do it have not any clear understanding of the fundamental design principles of their work. Most of the abstract mathematical and theoretical work is sterile because it has no point of contact with real computing.

-- Christopher Strachey

What can be modelled in LePUS3/Class-Z?

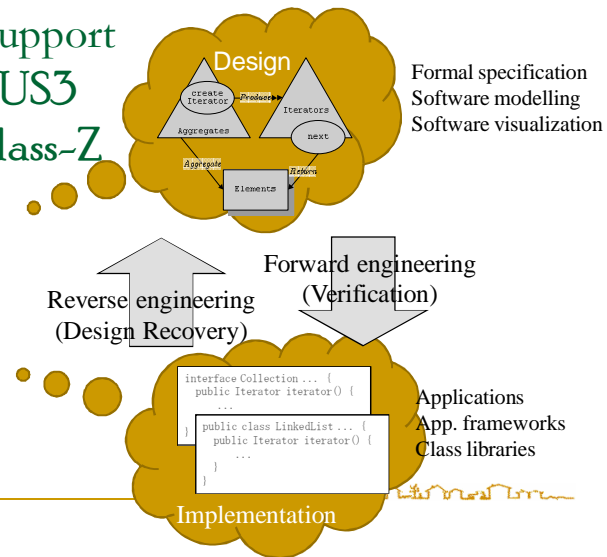


What *cannot* be modelled in LePUS3/Class-Z?

- Temporal relations
 - 'Method x should be called *before* method y'
 - No collaboration/interaction diagrams, flow charts, statecharts, ...
 - Statements about specific objects
- Strategic design
 - Architectural styles
 - Components
- Programs in procedural/functional/other programming paradigms
 - LePUS3 and Class-Z model object-oriented programs

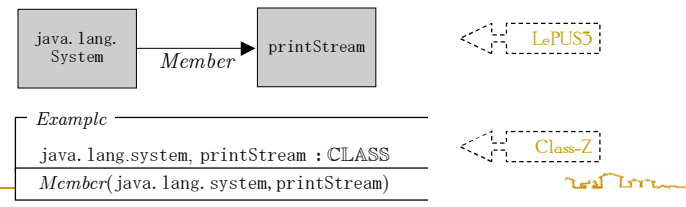
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Tool support in LePUS3 and Class-Z



LePUS3 vs. Class-Z

- Specifications can be expressed in one of two ways:
 - LePUS3: Visual, similar to UML Class Diagrams
 - Class-Z: symbolic, similar to Z
- Students are only required to learn one of the notations



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The genealogy of LePUS3 and Class-Z

- Definition: As a subset of first-order predicate calculus (classical logic)
- Official reference manual:
 - A.H. Eden, E. Gasparis, J. Nicholson. "LePUS3 and Class-Z Reference Manual". University of Essex, Tech. Rep. CSM-474, ISSN 1744-8050 (2007). <http://lepus.org.uk/ref/refman/refman.xml>
- Historical roots:
 - LePUS3: LePUS [Eden 2001]—LanguagE for Pattern Uniform Specification
 - Class-Z: Z [Spivey]

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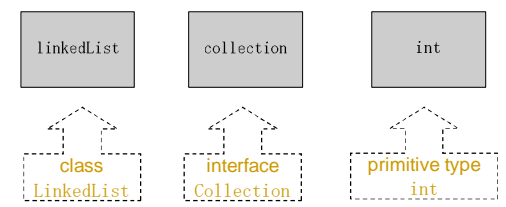
Modelling small programs in LePUS3 and Class-Z

- Class and signature constants
- Unary relation symbols
- Binary relation symbols

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Modelling individual classes

- class constant:** represents any specific static type such as a class, Java interface, and primitive types



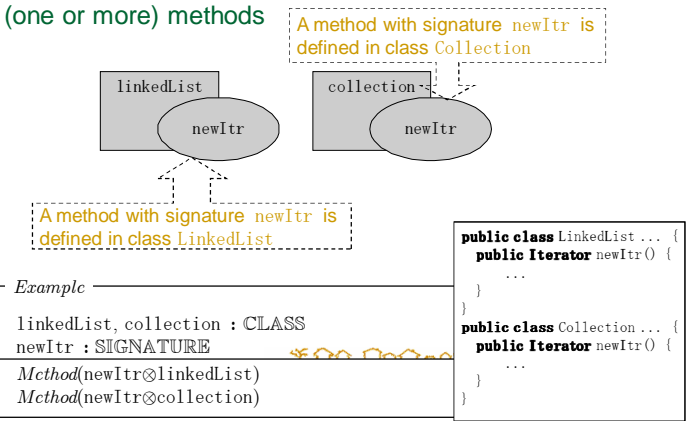
Example

```
LinkedList, collection, int : CLASS
```

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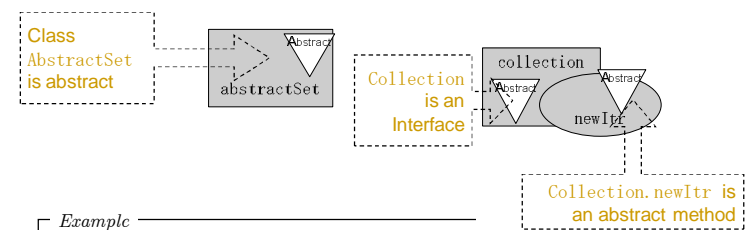
Modelling individual methods

- signature constant:** represents a specific 'signature' of (one or more) methods



Modelling properties

- Unary relation:** represents a property



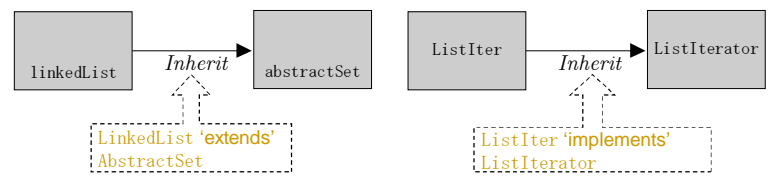
Example

```

abstractSet, collection : CLASS
newItr : SIGNATURE
Abstract(abstractSet)
Abstract(collection)
Abstract(newItr@collection)
    
```

Modelling relations between individuals

- **Binary relation:** represents a relation between two individuals



Example

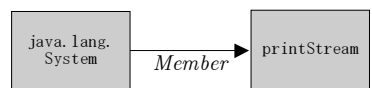
linkedList, abstractSet, ListItr, ListIterator : CLASS

Inherit(linkedList,abstractSet)

Inherit(ListItr,ListIterator)

Binary relations: Member

```
public class System {
    ...
    public static PrintStream out;
    ...
}
```

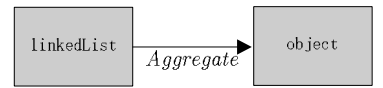


Example

java.lang.system, printStream : CLASS

Member(java.lang.system, printStream)

Binary relations: Aggregate



Example

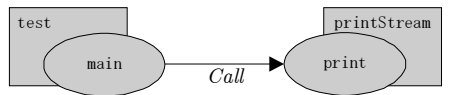
linkedList, object : CLASS

Aggregate(linkedList, object)

Binary relations: Call

- Note that the *Call* relation abstracts away all information about the control-flow

```
public class Test {
    public static void main(String[] args) {
        if (args.length == 0)
            System.out.print("Insufficient arguments");
        ...
    }
}
```



Example

test, printStream : CLASS

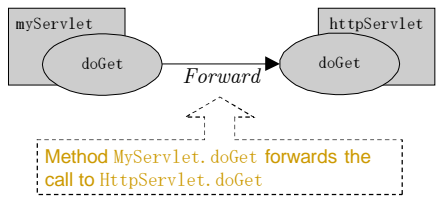
main, print : SIGNATURE

Call(main@test, print@printStream)

Binary relations: *Forward*

```
public class MyServlet extends HttpServlet {
    public void doGet(HttpServletRequest request, HttpServletResponse response) {
        super.doGet(request, response);
    }
}
```

Forward:
A special kind of a *Call* relation in which the formal arguments are passed on to a method with same signature

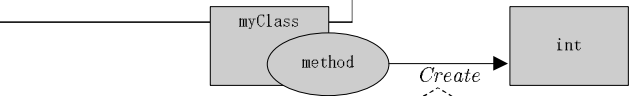


Method MyServlet.doGet forwards the call to HttpServlet.doGet

Example
myServlet, httpServlet : CLASS
doGet : SIGNATURE
Forward(doGet@myServlet, doGet@httpServlet)

Binary relations: *Create*

```
public class MyClass {
    public void method() {
        ... if ... else ...
        ... for (int index = 0; ...) ...
    }
}
```



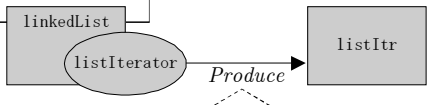
Method MyClass.method may create an integer

Example
linkedList, listItr : CLASS
listIterator : SIGNATURE
Produce(listIterator@linkedList, listItr)

Binary relations: *Produce*

```
public class LinkedList { ...
    public ListIterator listIterator(int index) {
        if (1 < 0)
            return new ListItr(index);
    } ...
}
```

Produce:
A special kind of a *Create* relation in which the new object is returned (typical to 'factory methods')



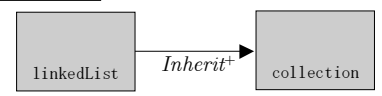
Method LinkedList.listIterator may create and return a new ListItr

Example
linkedList, listItr : CLASS
listIterator : SIGNATURE
Produce(listIterator@linkedList, listItr)

Modelling indirect relations

- **Transitive relation:** represents possibly indirect relation (the 'transitive closure' of a binary relation)

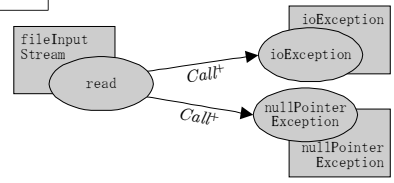
```
interface Collection { ...
class AbstractList implements Collection { ...
class AbstractSet extends AbstractList ...
class LinkedList extends AbstractSet ...
```



Example
linkedList, collection : CLASS
Inherit+(linkedList, collection)

Transitive relations II

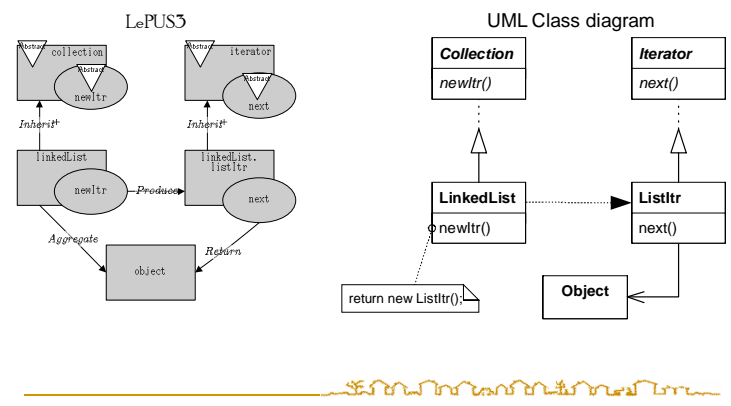
```
public class FileInputStream... {
    public int read(byte[] b)
        throws IOException, NullPointerException {
        ...
    }
}
```



Example

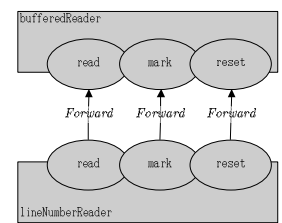
```
fileInputStream, ioException, nullPointerException : CLASS
read, nullPointerException, ioException : SIGNATURE
Call+(read@fileInputStream, ioException@ioException)
Call+(read@fileInputStream, nullPointerException@nullPointerException)
```

Case Study I: LinkedList and ListItr



Case Study II: java.io.XXReader classes

```
public class LineNumberReader
    extends BufferedReader { ...
    public void read() { ...
        super.read(); ...
    } ...
    public void mark(int readAheadLimit) { ...
        super.mark(readAheadLimit); ...
    } ...
    public void reset() { ...
        super.reset(); ...
    } ...
}
```



ReaderExample

```
bufferedReader, lineNumberReader : CLASS
read, mark, reset : SIGNATURE
Forward(read@lineNumberReader, read@bufferedReader)
Forward(mark@lineNumberReader, mark@bufferedReader)
Forward(reset@lineNumberReader, reset@bufferedReader)
```

Exercise

- “Translate” the LePUS3 chart in the case study into a Class-Z specification
- Use either Class-Z or LePUS to model three DIFFERENT specifications of the classes Collection, Iterator, LinkedList, and ListItr in the package java.util.
 - Each specification should include one or more of the methods defined in these classes. Which ones did you choose to model and why?
 - Note that each specification may contain a different set of relations
 - Note that each specification must be SATISFIED by the classes in java.util!

Exercise (Cont.)

- Which one is the most correct description of the purpose of a LePUS/Class-Z specification?
 1. Each specification is model of a particular implementation
 2. Each specification models an one or more possible implementations
 3. Each specification models an aspect of one implementation abstracted for a particular purpose
 4. Each specification models an aspect of one or more possible implementations abstracted for a particular purpose

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Exercise (Cont.)

- How many ways can you model a Java program in which class `MyClass` has a method therein with the signature `method(String arg)` which throws an exception of class `MyException` in LePUS3 or Class-Z?

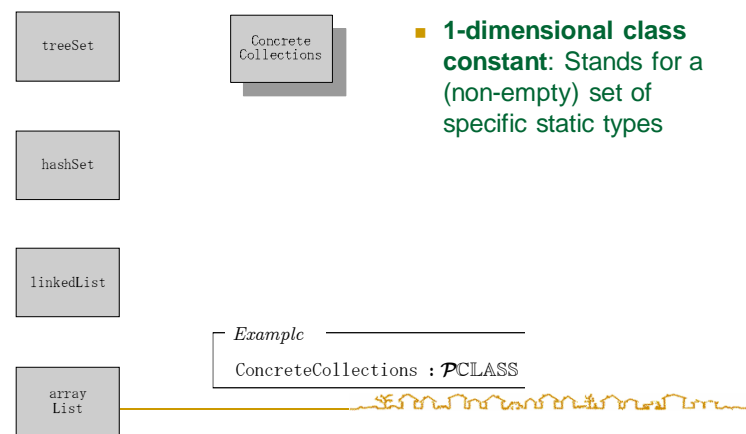
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Modelling large programs in LePUS3 and Class-Z

Hierarchy constant
1-dim class and signature constants
Total and Isomorphic predicates

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Modelling sets of classes



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Modelling sets of methods (one signature)

- **Clan:** A set of methods with same signature

Example

```
ConcreteCollections : PCCLASS
newItr : SIGNATURE
All(Method, newItr@ConcreteCollections)
```

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Modelling sets of methods (many signatures)

- **1-dimensional signature constant:** Stands for a (non-empty) set of specific method signatures



Example

```
1-DimSignatureConstant : PSIGNATURE
```

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Modelling sets of methods (many signatures)

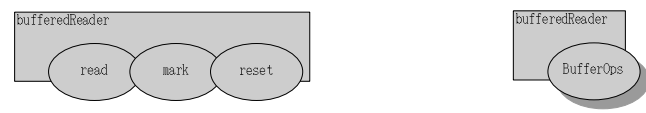
- **Tribe:** A set of methods in same class

Example

```
httpServlet : CLASS
ServletOps : PSIGNATURE
All(Method, ServletOps@httpServlet)
```

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Modelling sets of methods (many signatures): example



Example

```
BufferOps : PSIGNATURE
bufferedReader : CLASS
All(Method, BufferOps@bufferedReader)
```

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Modelling relations between sets: Total

Every element in Domain is in relation with some element in Range

$Total(BinaryRelation, Domain, Range)$

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Total predicate: example

Example

```
ConcreteCollections : PCCLASS
collection : CLASS
Total(Inherit+, ConcreteCollections, collection)
```

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Total predicate: example II

Example

```
ConcreteCollections : PCCLASS
object : CLASS
Total(Aggregate, ConcreteCollections, object)
```

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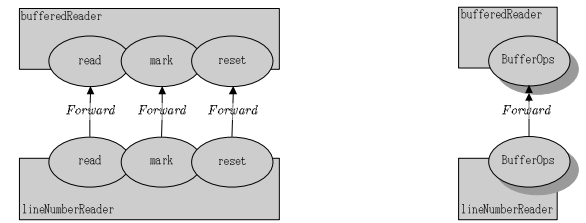
Modelling relations between sets: Isomorphic

Every element in Domain is in relation with a unique element in Range

$Isomorphic(BinaryRelation, Domain, Range)$

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Isomorphic predicate: example I

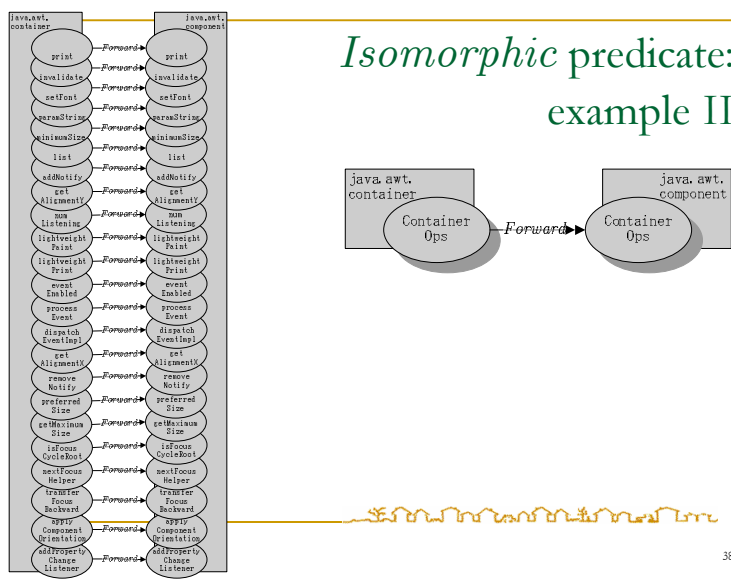


Example

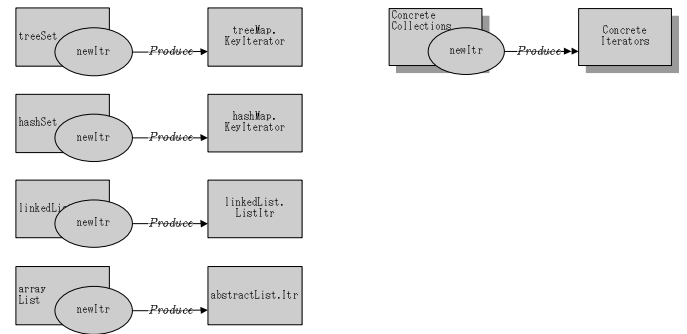
bufferedReader, lineNumberReader : CLASS
 BufferOps : PSIGNATURE

Inherit(lineNumberReader,bufferedReader)
 Isomorphic(Forward, ServletOps⊗lineNumberReader, ServletOps⊗bufferedReader)

Isomorphic predicate: example II



Case study: collections & iterators in java.util

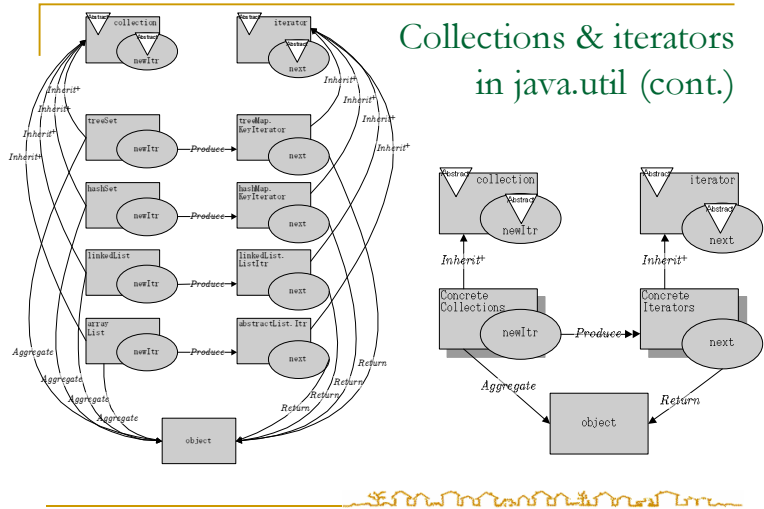


Example

ConcreteCollections, ConcreteIterators : PCLASS

Isomorphic(Produce, newItr⊗ConcreteCollections, ConcreteIterators)

Collections & iterators in java.util (cont.)



Exercise

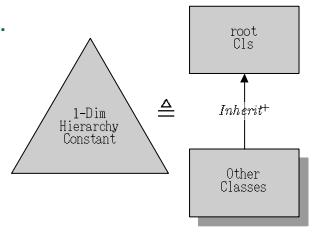
- Translate the specification of collections and iterators to UML



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Modelling class hierarchies

- 1-dimensional hierarchy constant:** a set of classes s.t. all inherit from one

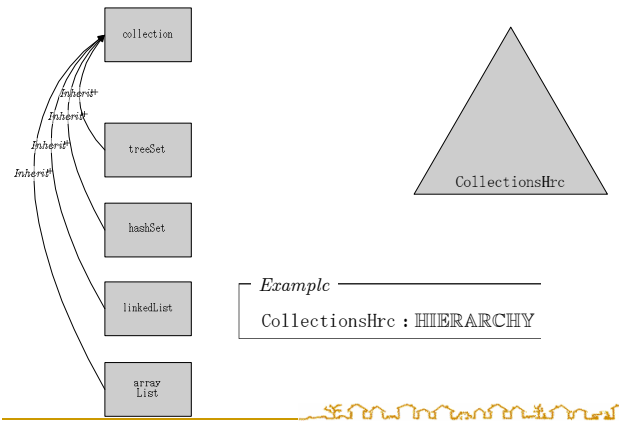


Example
Hierarchy : HIERARCHY



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Hierarchy: example

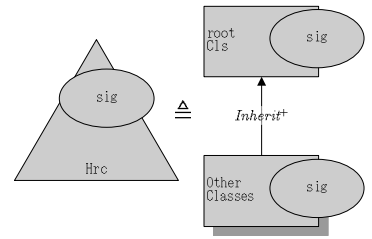


Example
CollectionsHrc : HIERARCHY

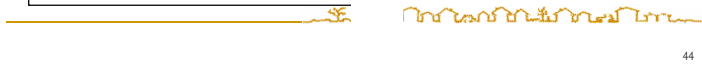


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Modelling sets of methods revisited

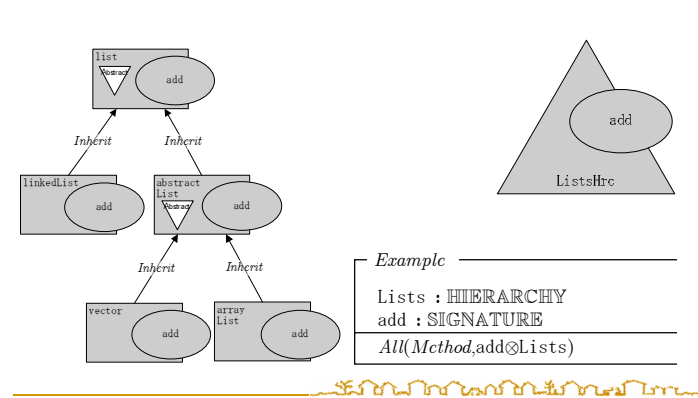


Example
Hrc : HIERARCHY
sig : SIGNATURE
All(Method, sig@Hrc)



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Example: the Lists hierarchy

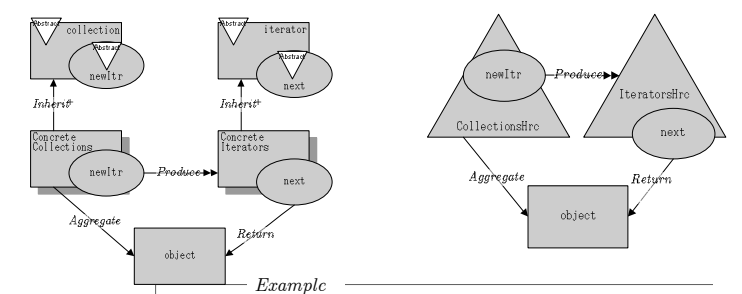


Example

Lists : HIERARCHY
 add : SIGNATURE
 All(Method, add@Lists)

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Case study: collections & iterators in java.util



Example

CollectionsShrc, IteratorsShrc : HIERARCHY
 next, newItr : SIGNATURE
 object : CLASS

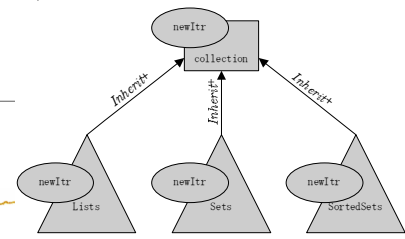
Isomorphic(Produce, newItr@CollectionsShrc, IteratorsShrc)
 Total(Return, next@IteratorsShrc, object)
 Total(Aggregate, CollectionsShrc, IteratorsShrc)

Example: lists, sets, and sorted sets

Example

Lists, Sets, SortedSets : HIERARCHY
 newItr : SIGNATURE
 collection : CLASS

Total(Inherit+, Lists, collection)
 Total(Inherit+, Sets, collection)
 Total(Inherit+, SortedSets, collection)
 Method(newItr@collection)
 All(Method, newItr@Lists)
 All(Method, newItr@Sets)
 All(Method, newItr@SortedSets)

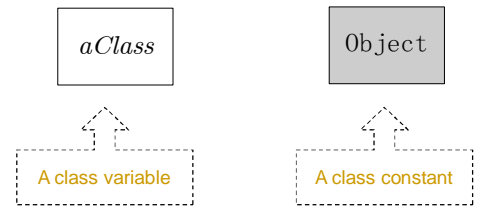


Modelling application frameworks

Variables

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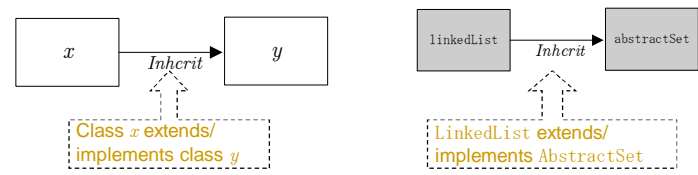
Variables vs. constants



Example
`aClass, Object : CLASS`

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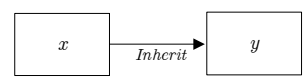
Variables vs. constants II



Example
`LinkedList, abstractSet, x, y : CLASS`
`Inherit(LinkedList, abstractSet)`
`Inherit(x, y)`

Assignments

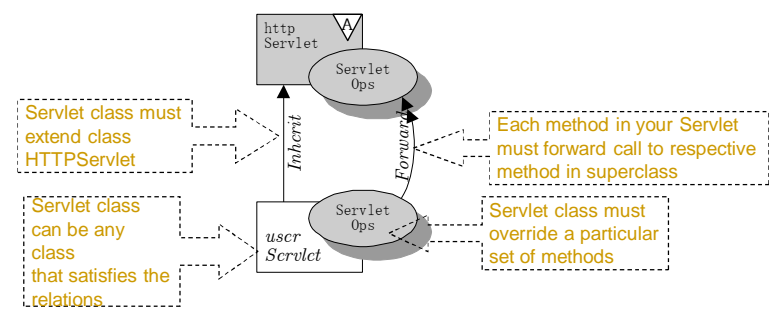
- A specification with variables is only meaningful wrt a specific **assignment**
- Example: Assignment-1
 - *x* is assigned to LinkedList
 - *y* is assigned to AbstractSet
- Example: Assignment-2
 - *y* is assigned to LinkedList
 - *x* is assigned to AbstractSet
- Assignment-1 is *satisfied* by java.util
- Assignment-2 is *satisfied* by java.util



Example
`x, y : CLASS`
`Inherit(x, y)`

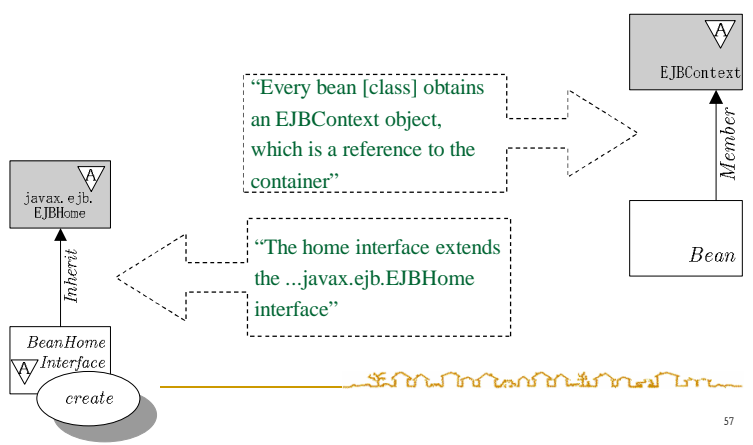
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Example: Java Servlets



JavaServlet
`httpServlet, usrServlet : CLASS`
`ServletOps : P(SIGNATURE)`
`Isomorphic(Forward, ServletOps@usrServlet, ServletOps@httpServlet)`
`Inherit(usrServlet, httpServlet)`

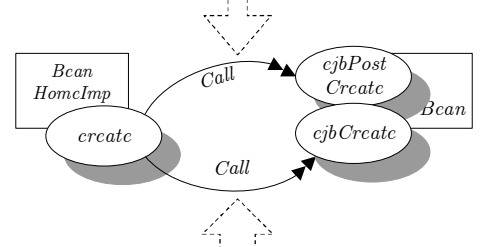
Modelling Enterprise JavaBeans I



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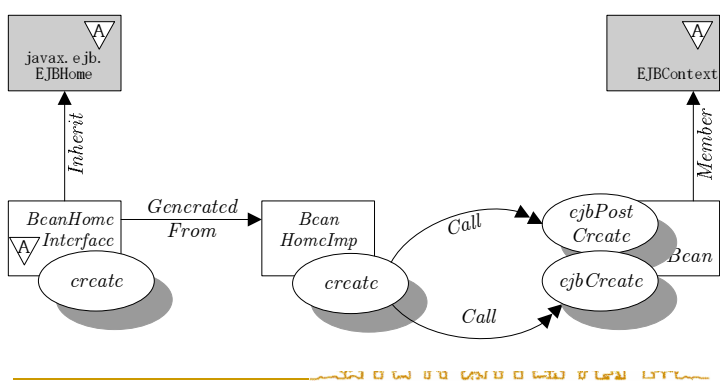
Modelling Enterprise JavaBeans II

“A home [interface] may have many create() methods, ... , each of which must have corresponding ejbCreate() and ejbPostCreate() methods in the bean class. The number and datatype of the arguments of each create() are left up to the bean developer



“When a create() method is invoked on the home interface, the container delegates the invocation to the corresponding ejbCreate() and ejbPostCreate() methods on the bean class”

Summary: Enterprise JavaBeans



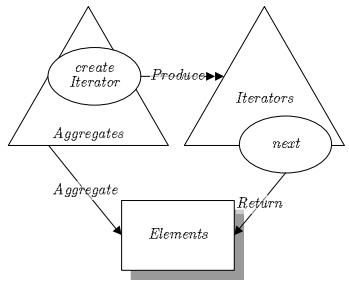
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Modelling design patterns

The ‘gang of four’ patterns:
 Iterator, Proxy, Composite, Observer,
 Factory Method, Adapter (Object), Adapter (Class), Strategy

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Iterator pattern



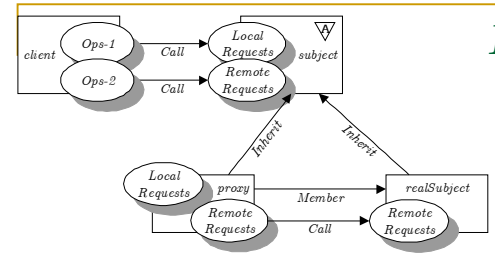
Iterator

Aggregates, Iterators : HIERARCHY
 createIterator, next : SIGNATURE
 Elements : PCCLASS

Isomorphic(Produce, createIterator@Aggregates, Iterators)
 Total(Return, next@Iterators, Elements)
 Total(Aggregate, Aggregates, Elements)

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Proxy pattern



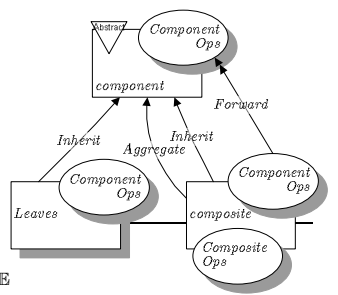
Proxy

client, subject, proxy, realSubject : CLASS
 Ops-1, Ops-2, LocalRequests, RemoteRequests : PSIGNATURE

Abstract(subject)
 Total(Call, Ops-1@client, LocalRequests@subject)
 Total(Call, Ops-2@Client, RemoteRequests@subject)
 Total(Call, RemoteRequests@proxy, RemoteRequests@realSubject)
 Method(LocalRequests@proxy)
 Member(proxy, realSubject)
 Inherit(proxy, subject)
 Inherit(realSubject, subject)

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Composite pattern



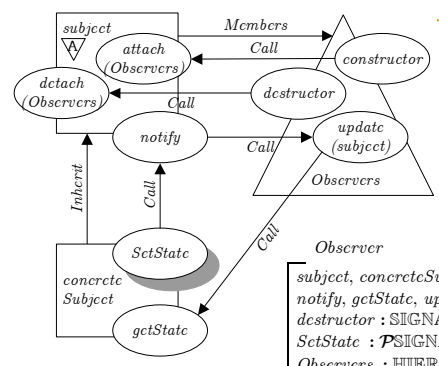
Composite

component, composite : CLASS
 Leaves : PCCLASS
 CompositeOps, ComponentOps : PSIGNATURE

Abstract(component)
 All(Method, ComponentOps@Leaves)
 All(Method, CompositeOps@composite)
 Inherit(composite, component)
 Total(Inherit, Leaves, component)
 Aggregate(composite, component)
 Isomorphic(Forward, ComponentOps@composite, ComponentOps@component)

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Observer pattern

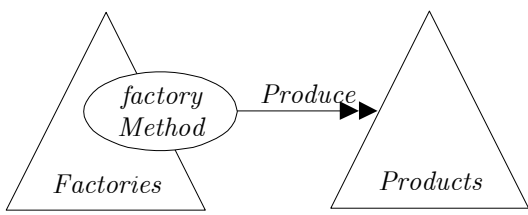


Observer

subject, concreteSubject : CLASS
 notify, getState, update, attach, detach, constructor, destructor : SIGNATURE
 SetState : PSIGNATURE
 Observers : HIERARCHY

Abstract(subject)
 Inherit(concreteSubject, subject)
 Total(Call, SetState@concreteSubject, notify@subject)
 Total(Call, notify@subject, update@Observers)
 Total(Call, update@Observers, getState@concreteSubject)
 Total(Call, constructor@Observers, attach@subject)
 Total(Call, destructor@Observers, detach@subject)
 Members(subject, Observers)

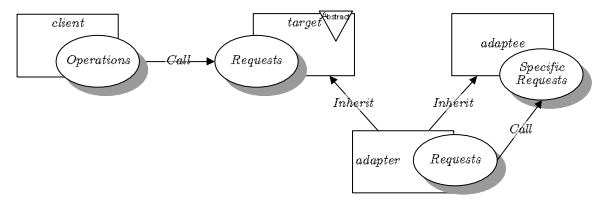
Factory Method pattern



<i>FactoryMethod</i>
<i>Factories, Products</i> : HIERARCHY <i>factoryMethod</i> : SIGNATURE
<i>Isomorphic(Produce, factoryMethod ⊙ Factories, Products)</i>

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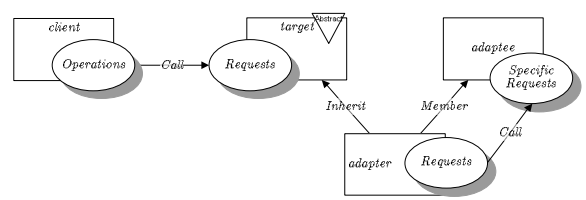
Adapter (Class) pattern



<i>ClassAdapter</i>
<i>client, target, adapter, adaptec</i> : CLASS <i>Operations, Requests, SpecificRequests</i> : PSIGNATURE
<i>Abstract(target)</i> <i>Total(Call, Operations ⊙ client, Requests ⊙ target)</i> <i>Total(Call, Requests ⊙ adapter, SpecificRequests ⊙ adaptec)</i> <i>Inherit(adapter, target)</i> <i>Inherit(adapter, adaptec)</i>

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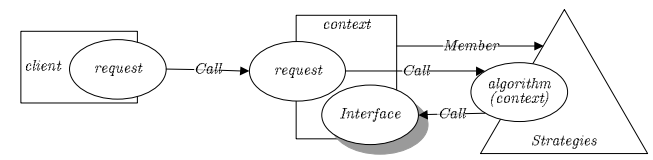
Adapter (Object) pattern



<i>ObjectAdapter</i>
<i>client, target, adapter, adaptec</i> : CLASS <i>Operations, Requests, SpecificRequests</i> : P(SIGNATURE)
<i>Abstract(target)</i> <i>Total(Call, Operations ⊙ client, Requests ⊙ target)</i> <i>Total(Call, Requests ⊙ adapter, SpecificRequests ⊙ adaptec)</i> <i>Inherit(adapter, target)</i> <i>Member(adapter, adaptec)</i>

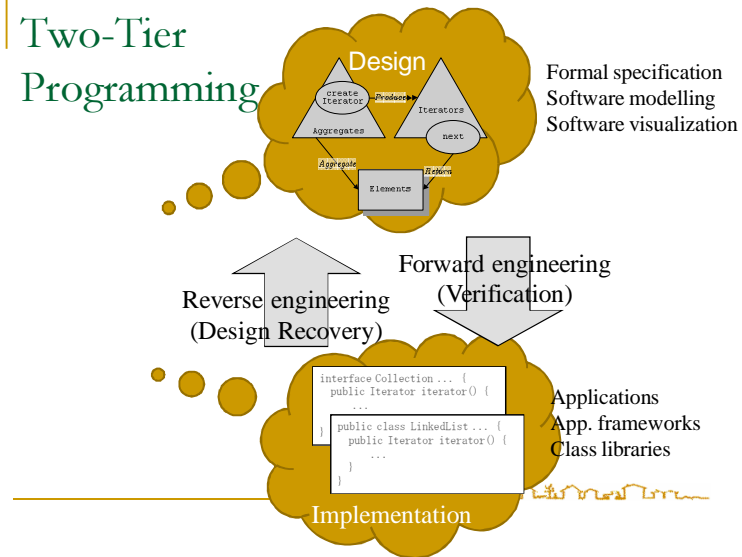
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Strategy pattern



<i>Strategy</i>
<i>client, context</i> : CLASS <i>request, algorithm</i> : SIGNATURE <i>Interface</i> : P(SIGNATURE) <i>Strategies</i> : HIERARCHY
<i>Member(context, Strategies)</i> <i>Call(request ⊙ client, request ⊙ context)</i> <i>Call(request ⊙ context, algorithm ⊙ Strategies)</i> <i>Total(Call, algorithm ⊙ Strategies, Interface ⊙ context)</i>

Tool support in LePUS3 and Class-Z

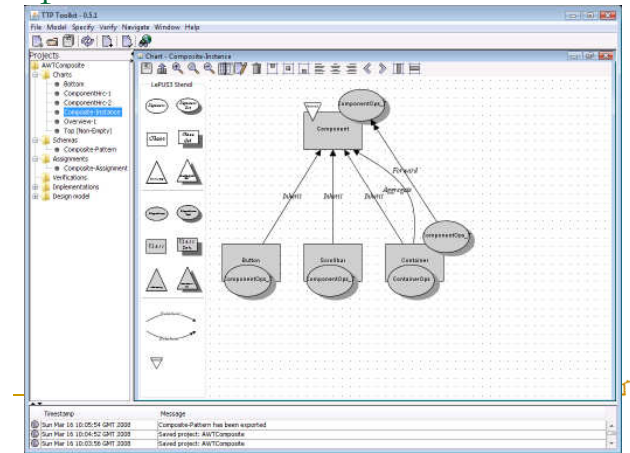


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The Two-Tier Programming Toolkit

- Round-trip engineering
- Supports:
 - Specification & verification (forward engineering)
 - Visualization (reverse engineering)
- <http://ttp.essex.ac.uk>

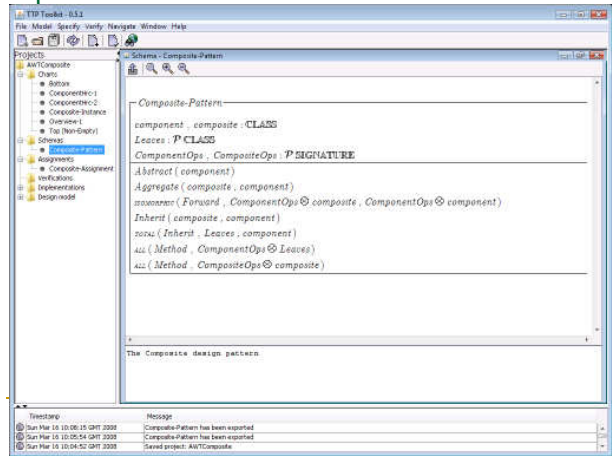
The TTP Toolkit (cont.): Specification in LePUS3



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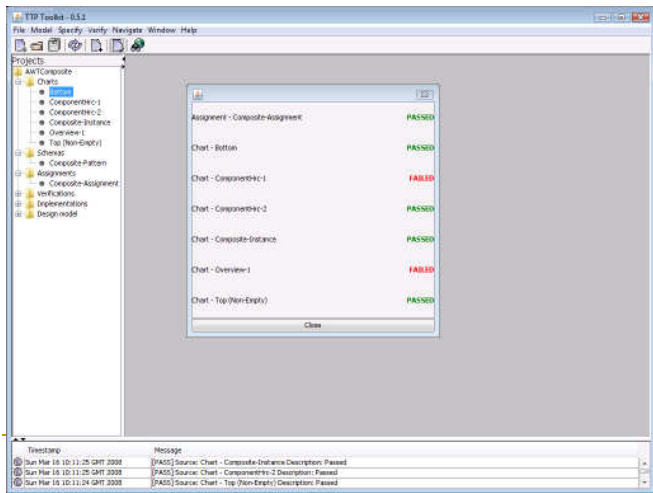
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The TTP Toolkit (cont.): Specification in Class-Z



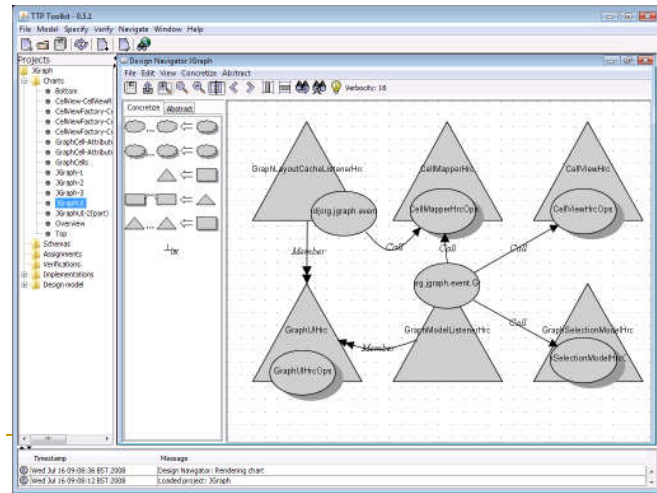
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The TTP Toolkit (cont.): Verification



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The TTP Toolkit (cont.): Visualization



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Exercises

1. Summarize the differences between LePUS3/Class-Z and UML:
 - 1.1 Compare the LePUS3 chart with the UML Class diagram of LinkedList and the ListTr classes
 - 1.2 Use UML to model the Collection and the Iterator hierarchies in Java.util. How is this diagram different from the LePUS3/Class-Z specification?
 - 1.3 Use UML to model Java Servlets. How is this diagram different from the LePUS3/Class-Z specification?
 - 1.4 Use UML to model one of the design patterns. How is this diagram different from the LePUS3/Class-Z specification?
2. List four abstraction mechanisms in LePUS3/Class-Z

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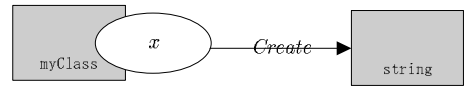
Exercises (cont.)

- 3. Compare the LePUS3/Class-Z Specification of each one of the design patterns to the description in Gamma et al. 1995
 - 3.1 What is the book saying that the chart/schema does not say?
 - 3.2 What is the chart/schema saying that the book does not say?
 - 3.3 What are the advantages of the book over the chart?
 - 3.4 What are the advantages of the chart over the book?

Exercises (cont.)

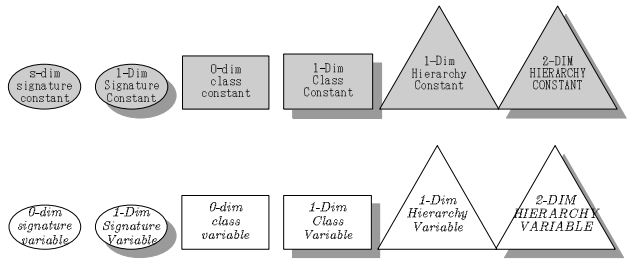
- 4. Specify in LePUS3/Class-Z the following statements:
 - 4.1 "There exists a method in class MyClass which creates instances of class String"

Answer:

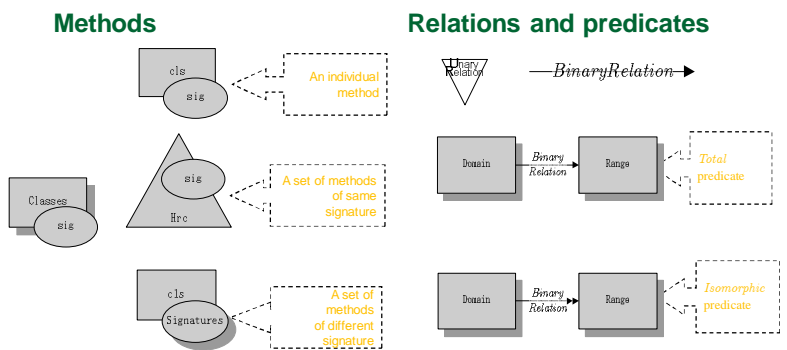


LePUS3 quick reference

■ constants and variables



LePUS3 quick reference (cont.)



References

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- A.H. Eden, J. Nicholson. *Object-oriented modelling: Theory and Practice*. Unpublished manuscript (ask me for a copy)
- A.H. Eden, E. Gasparis, J. Nicholson. "[LePUS3 and Class-Z Reference Manual](http://www.lepus.org.uk/ref/refman/refman.xml)". University of Essex, Tech. Rep. CSM-474, ISSN 1744-8050 (2007). <<http://www.lepus.org.uk/ref/refman/refman.xml>>
- A.H. Eden, E. Gasparis, J. Nicholson. "[The 'Gang of Four' Companion: Formal specification of design patterns in LePUS3 and Class-Z.](http://www.lepus.org.uk/ref/companion/index.xml)" University of Essex, Tech. Rep. CSM-472, ISSN 1744-8050 (2007). <<http://www.lepus.org.uk/ref/companion/index.xml>>
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